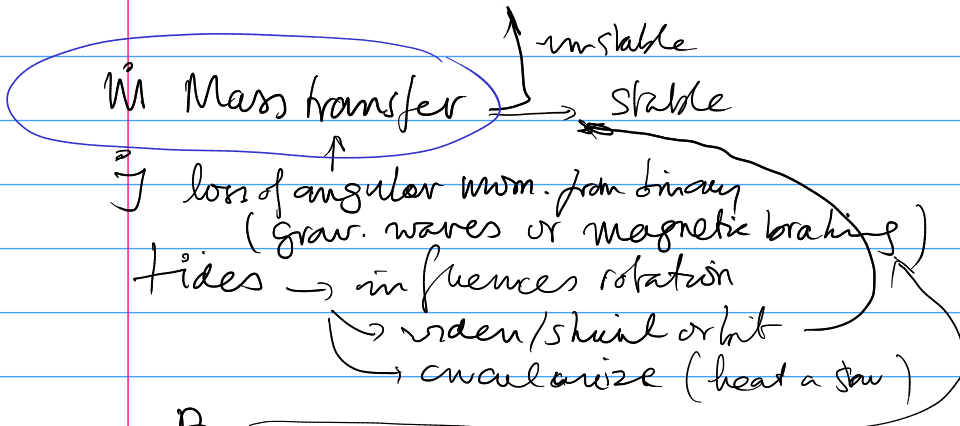


Differences from single star evolution?

Common envelope



B "slam a companion"

SN → unbind binary?
pollute the companion

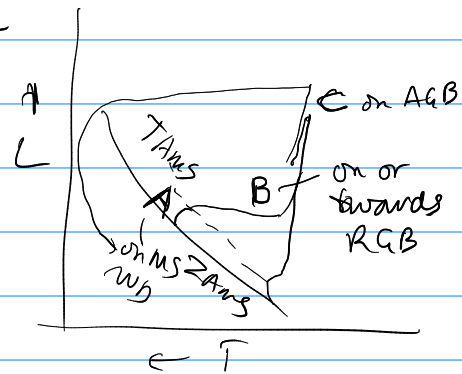
When we would get mass transfer

→ shrink orbit (must have short P to start with)

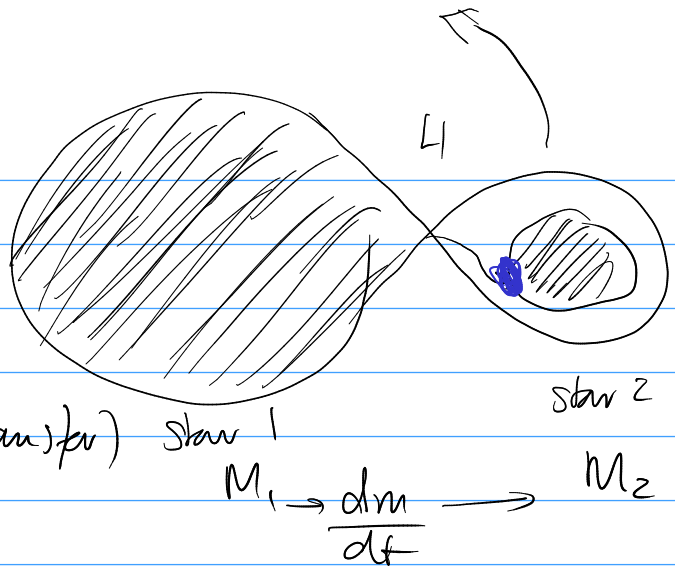
→ expand your star

↓ Which star? → more massive one

When? → on way to red giant most likely



Transfer mass
 → what happens?



$$\dot{m} = -\dot{M}_1 = +\dot{M}_2$$

(conservative mass transfer) Star 1

angular momentum

energy? no, lose too much, hard to calculate

$$L = \frac{M_1 M_2}{M_1 + M_2} \sqrt{G(M_1 + M_2)a} = \frac{M_1 M_2}{M} \sqrt{G M a}$$

$$\frac{\dot{L}}{L} = \frac{\dot{M}_1}{M_1} + \frac{\dot{M}_2}{M_2} + \frac{1}{2} \frac{\dot{a}}{a} = 0$$

$$\frac{\dot{a}}{a} = 2 \frac{\dot{m} (M_2 - M_1)}{M_1 M_2}$$

orbit shrinks
 if $M_1 > M_2$
 from more massive to less massive

Stable ① look at Roche lobe $\frac{R_L}{a} = f(q)$

⇒ shrinks faster (L_1 moves in)

② look at stellar radius

I. initially a little smaller

II on HE (dynamical scale) expand a little but still smaller than before

III If convective envelope on turnover time back to original radius or a bit bigger

unstable on conv. turnover time → fast, ~ dynamical

III If radiative env. on thermal timescale back to original radius

↓
 unstable on thermal timescale

Dynamically unstable

What happens? Common envelope

~ merger

If stars are similar (both MS, 2 wh, etc)

→ proper merger →

rapidly rotating remnant

differentially → magnetic field

Some mass loss → ~1% (from simulations)

If one or both are giants

→ can eject the envelope

end w/ binary core (s)

Appeal to basic energetics

(assume fast, not much en. con)

$$\text{Before } E_{\text{tot, initial}} = -\frac{GM_1 M_2}{2a_i}$$

$$\text{After } E_{\text{tot, final}} = -\frac{GM_{\text{core}} M_2}{2a_f}$$

$$\text{Eject envelope } E_{\text{env}} = \frac{GM_{1, \text{initial}} M_{1, \text{env}}}{\lambda R_{1, \text{initial}}}$$

$$\text{Assume efficiency } \alpha_{\text{CE}} = \frac{E_{\text{env}}}{E_{\text{orb, f}} - E_{\text{orb, i}}}$$

$$\frac{a_f}{a_i} = \frac{M_{1, f}}{M_{1, i}} \left[1 - \frac{2}{\alpha_{\text{CE}}} \frac{a_{1, i}}{R_{1, i}} \frac{M_{1, i} M_{1, \text{env}}}{M_2} \right]^{-1}$$

↑
if Roche-lobe filling
→ f(q)